

1996 AJHSME Problems

Problem 1

How many positive factors of 36 are also multiples of 4?

- (A) 2 (B) 3 (C) 4 (D) 5 (E) 6

Solution

Problem 2

Jose, Thuy, and Kareem each start with the number 10. Jose subtracts 1 from the number 10, doubles his answer, and then adds 2. Thuy doubles the number 10, subtracts 1 from her answer, and then adds 2. Kareem subtracts 1 from the number 10, adds 2 to his number, and then doubles the result. Who gets the largest final answer?

- (A) Jose (B) Thuy (C) Kareem (D) Jose and Thuy (E) Thuy and Kareem

Solution

Problem 3

The 64 whole numbers from 1 through 64 are written, one per square, on a checkerboard (an 8 by 8 array of 64 squares). The first 8 numbers are written in order across the first row, the next 8 across the second row, and so on. After all 64 numbers are written, the sum of the numbers in the four corners will be

- (A) 130 (B) 131 (C) 132 (D) 133 (E) 134

Solution

Problem 4

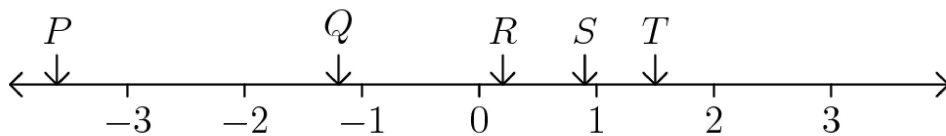
$$\frac{2 + 4 + 6 + \cdots + 34}{3 + 6 + 9 + \cdots + 51} =$$

- (A) $\frac{1}{3}$ (B) $\frac{2}{3}$ (C) $\frac{3}{2}$ (D) $\frac{17}{3}$ (E) $\frac{34}{3}$

Solution

Problem 5

The letters P , Q , R , S , and T represent numbers located on the number line as shown.



Which of the following expressions represents a negative number?

- (A) $P - Q$ (B) $P \cdot Q$ (C) $\frac{S}{Q} \cdot P$ (D) $\frac{R}{P \cdot Q}$ (E) $\frac{S + T}{R}$

Solution

Problem 6

What is the smallest result that can be obtained from the following process?

- Choose three different numbers from the set $\{3, 5, 7, 11, 13, 17\}$.
- Add two of these numbers.
- Multiply their sum by the third number.

- (A) 15 (B) 30 (C) 36 (D) 50 (E) 56

Solution

Problem 7

Brent has goldfish that quadruple (become four times as many) every month, and Gretel has goldfish that double every month. If Brent has 4 goldfish at the same time that Gretel has 128 goldfish, then in how many months from that time will they have the same number of goldfish?

- (A) 4 (B) 5 (C) 6 (D) 7 (E) 8

Solution

Problem 8

Points A and B are 10 units apart. Points B and C are 4 units apart. Points C and D are 3 units apart. If A and D are as close as possible, then the number of units between them is

- (A) 0 (B) 3 (C) 9 (D) 11 (E) 17

Solution

Problem 9

If 5 times a number is 2, then 100 times the reciprocal of the number is

- (A) 2.5 (B) 40 (C) 50 (D) 250 (E) 500

Solution

Problem 10

When Walter drove up to the gasoline pump, he noticed that his gasoline tank was $\frac{1}{8}$ full. He purchased 7.5 gallons of gasoline for \$10. With this additional gasoline, his gasoline tank was then $\frac{5}{8}$ full. The number of gallons of gasoline his tank holds when it is full is

- (A) 8.75 (B) 10 (C) 11.5 (D) 15 (E) 22.5

Solution

Problem 11

Let x be the number $0.\underbrace{0000\dots0000}_{1996 \text{ zeros}}1$, where there are 1996 zeros after the decimal point. Which of the following expressions represents the largest number?

- (A) $3 + x$ (B) $3 - x$ (C) $3 \cdot x$ (D) $3/x$ (E) $x/3$

Solution

Problem 12

What number should be removed from the list 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11 so that the average of the remaining numbers is 6.1?

- (A) 4 (B) 5 (C) 6 (D) 7 (E) 8

Solution

Problem 13

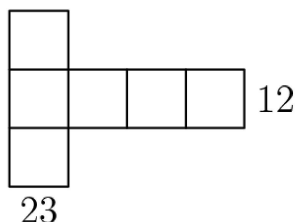
In the fall of 1996, a total of 800 students participated in an annual school clean-up day. The organizers of the event expect that in each of the years 1997, 1998, and 1999, participation will increase by 50% over the previous year. The number of participants the organizers will expect in the fall of 1999 is

- (A) 1200 (B) 1500 (C) 2000 (D) 2400 (E) 2700

Solution

Problem 14

Six different digits from the set $\{1, 2, 3, 4, 5, 6, 7, 8, 9\}$ are placed in the squares in the figure shown so that the sum of the entries in the vertical column is 23 and the sum of the entries in the horizontal row is 12. The sum of the six digits used is



- (A) 27 (B) 29 (C) 31 (D) 33 (E) 35

Solution

Problem 15

The remainder when the product $1492 \cdot 1776 \cdot 1812 \cdot 1996$ is divided by 5 is

- (A) 0 (B) 1 (C) 2 (D) 3 (E) 4

Solution

Problem 16

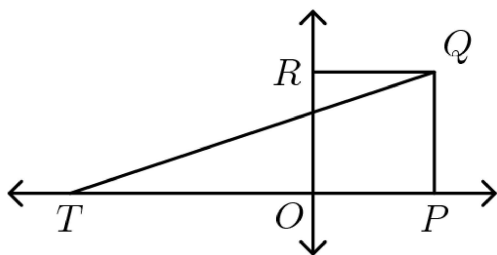
$1 - 2 - 3 + 4 + 5 - 6 - 7 + 8 + 9 - 10 - 11 + \cdots + 1992 + 1993 - 1994 - 1995 + 1996 =$

- (A) -998 (B) -1 (C) 0 (D) 1 (E) 998

Solution

Problem 17

Figure $OPQR$ is a square. Point O is the origin, and point Q has coordinates $(2,2)$. What are the coordinates for T so that the area of triangle PQT equals the area of square $OPQR$?



NOT TO SCALE

- (A) $(-6, 0)$ (B) $(-4, 0)$ (C) $(-2, 0)$ (D) $(2, 0)$ (E) $(4, 0)$

Solution

Problem 18

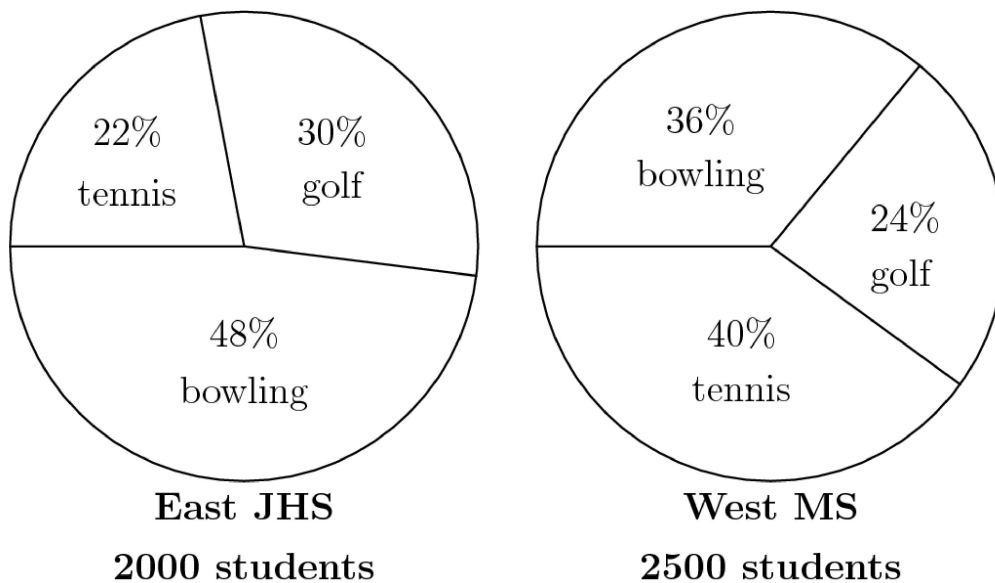
Ana's monthly salary was \$2000 in May. In June she received a 20% raise. In July she received a 20% pay cut. After the two changes in June and July, Ana's monthly salary was

- (A) 1920 dollars (B) 1980 dollars (C) 2000 dollars (D) 2020 dollars (E) 2040 dollars

Solution

Problem 19

The pie charts below indicate the percent of students who prefer golf, bowling, or tennis at East Junior High School and West Middle School. The total number of students at East is 2000 and at West, 2500. In the two schools combined, the percent of students who prefer tennis is



- (A) 30% (B) 31% (C) 32% (D) 33% (E) 34%

Solution

Problem 20

Suppose there is a special key on a calculator that replaces the number x currently displayed with the number given by the formula $1/(1 - x)$. For example, if the calculator is displaying 2 and the special key is pressed, then the calculator will display -1 since

$1/(1 - 2) = -1$. Now suppose that the calculator is displaying 5. After the special key is pressed 100 times in a row, the calculator will display

- (A) -0.25 (B) 0 (C) 0.8 (D) 1.25 (E) 5

Solution

Problem 21

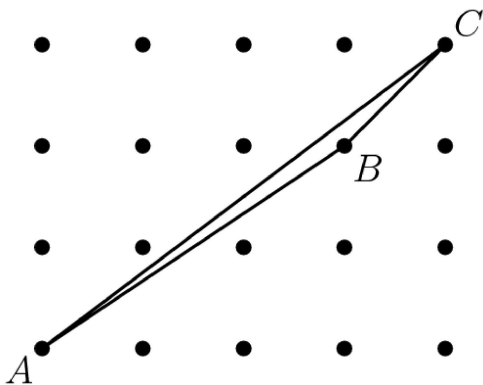
How many subsets containing three different numbers can be selected from the set $\{89, 95, 99, 132, 166, 173\}$ so that the sum of the three numbers is even?

- (A) 6 (B) 8 (C) 10 (D) 12 (E) 24

Solution

Problem 22

The horizontal and vertical distances between adjacent points equal 1 unit. The area of triangle ABC is



- (A) $1/4$ (B) $1/2$ (C) $3/4$ (D) 1 (E) $5/4$

Solution

Problem 23

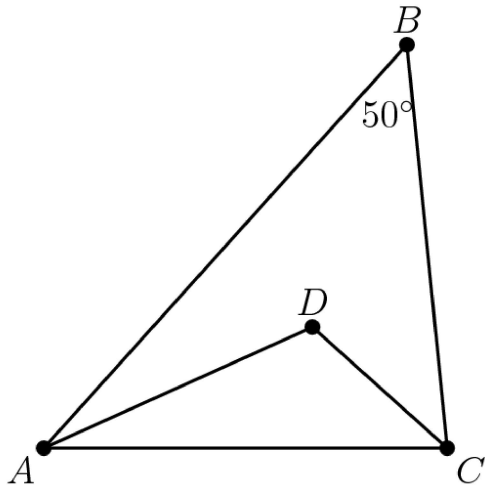
The manager of a company planned to distribute a \$50 bonus to each employee from the company fund, but the fund contained \$5 less than what was needed. Instead the manager gave each employee a \$45 bonus and kept the remaining \$95 in the company fund. The amount of money in the company fund before any bonuses were paid was

- (A) 945 dollars (B) 950 dollars (C) 955 dollars (D) 990 dollars (E) 995 dollars

Solution

Problem 24

The measure of angle ABC is 50° , \overline{AD} bisects angle BAC , and \overline{DC} bisects angle BCA . The measure of angle ADC is



- (A) 90° (B) 100° (C) 115° (D) 122.5° (E) 125°

Solution

Problem 25

A point is chosen at random from within a circular region. What is the probability that the point is closer to the center of the region than it is to the boundary of the region?

- (A) $1/4$ (B) $1/3$ (C) $1/2$ (D) $2/3$ (E) $3/4$

Solution

1996 AJHSME Answer Key

1. B
2. C
3. A
4. B
5. A
6. C
7. B
8. B
9. D
10. D
11. D
12. B
13. E
14. B
15. E
16. C
17. C
18. A
19. C
20. A
21. D
22. B
23. E
24. C
25. A