

# 1997 AJHSME Problems

## Problem 1

$$\frac{1}{10} + \frac{9}{100} + \frac{9}{1000} + \frac{7}{10000} =$$

- (A) 0.0026    (B) 0.0197    (C) 0.1997    (D) 0.26    (E) 1.997

Solution

## Problem 2

Ahn chooses a two-digit integer, subtracts it from 200, and doubles the result. What is the largest number Ahn can get?

- (A) 200    (B) 202    (C) 220    (D) 380    (E) 398

Solution

## Problem 3

Which of the following numbers is the largest?

- (A) 0.97    (B) 0.979    (C) 0.9709    (D) 0.907    (E) 0.9089

Solution

## Problem 4

Julie is preparing a speech for her class. Her speech must last between one-half hour and three-quarters of an hour. The ideal rate of speech is 150 words per minute. If Julie speaks at the ideal rate, which of the following number of words would be an appropriate length for her speech?

- (A) 2250    (B) 3000    (C) 4200    (D) 4350    (E) 5650

Solution

## Problem 5

There are many two-digit multiples of 7, but only two of the multiples have a digit sum of 10. The sum of these two multiples of 7 is

- (A) 119    (B) 126    (C) 140    (D) 175    (E) 189

Solution

## Problem 6

In the number 74982.1035 the value of the *place* occupied by the digit 9 is how many times as great as the value of the *place* occupied by the digit 3?

- (A) 1,000    (B) 10,000    (C) 100,000    (D) 1,000,000    (E) 10,000,000

Solution

## Problem 7

The area of the smallest square that will contain a circle of radius 4 is

- (A) 8    (B) 16    (C) 32    (D) 64    (E) 128

Solution

## Problem 8

Walter gets up at 6:30 a.m., catches the school bus at 7:30 a.m., has 6 classes that last 50 minutes each, has 30 minutes for lunch, and has 2 hours additional time at school. He takes the bus home and arrives at 4:00 p.m. How many minutes has he spent on the bus?

- (A) 30    (B) 60    (C) 75    (D) 90    (E) 120

Solution

## Problem 9

Three students, with different names, line up in single file. What is the probability that they are in alphabetical order from front-to-back?

- (A)  $\frac{1}{12}$     (B)  $\frac{1}{9}$     (C)  $\frac{1}{6}$     (D)  $\frac{1}{3}$     (E)  $\frac{2}{3}$

Solution

## Problem 10

What fraction of this square region is shaded? Stripes are equal in width, and the figure is drawn to scale.



- (A)  $\frac{5}{12}$     (B)  $\frac{1}{2}$     (C)  $\frac{7}{12}$     (D)  $\frac{2}{3}$     (E)  $\frac{5}{6}$

Solution

### Problem 11

Let  $\boxed{N}$  mean the number of whole number divisors of  $N$ . For example,  $\boxed{3} = 2$  because 3 has two divisors, 1 and 3. Find the value of

$$\boxed{\boxed{11} \times \boxed{20}}.$$

- (A) 6    (B) 8    (C) 12    (D) 16    (E) 24

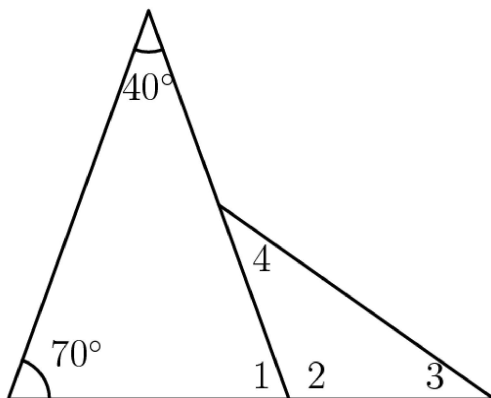
Solution

### Problem 12

$$\angle 1 + \angle 2 = 180^\circ$$

$$\angle 3 = \angle 4$$

Find  $\angle 4$ .



- (A)  $20^\circ$     (B)  $25^\circ$     (C)  $30^\circ$     (D)  $35^\circ$     (E)  $40^\circ$

Solution

### Problem 13

Three bags of jelly beans contain 26, 28, and 30 beans. The ratios of yellow beans to all beans in each of these bags are 50%, 25%, and 20%, respectively. All three bags of candy

are dumped into one bowl. Which of the following is closest to the ratio of yellow jelly beans to all beans in the bowl?

- (A) 31%    (B) 32%    (C) 33%    (D) 35%    (E) 95%

Solution

### Problem 14

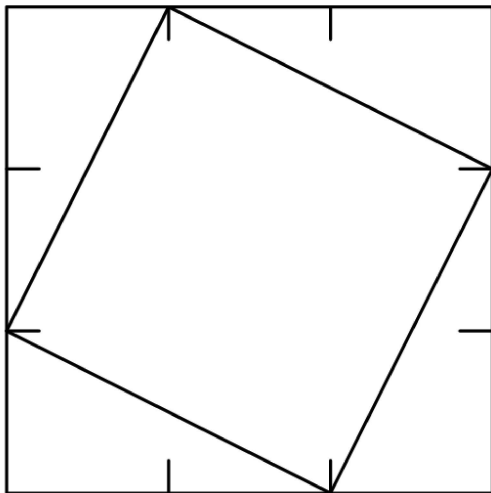
There is a set of five positive integers whose average (mean) is 5, whose median is 5, and whose only mode is 8. What is the difference between the largest and smallest integers in the set?

- (A) 3    (B) 5    (C) 6    (D) 7    (E) 8

Solution

### Problem 15

Each side of the large square in the figure is trisected (divided into three equal parts). The corners of an inscribed square are at these trisection points, as shown. The ratio of the area of the inscribed square to the area of the large square is



- (A)  $\frac{\sqrt{3}}{3}$     (B)  $\frac{5}{9}$     (C)  $\frac{2}{3}$     (D)  $\frac{\sqrt{5}}{3}$     (E)  $\frac{7}{9}$

Solution

### Problem 16

Penni Precisely buys \$100 worth of stock in each of three companies: Alabama Almonds, Boston Beans, and California Cauliflower. After one year, AA was up 20%, BB was down 25%,

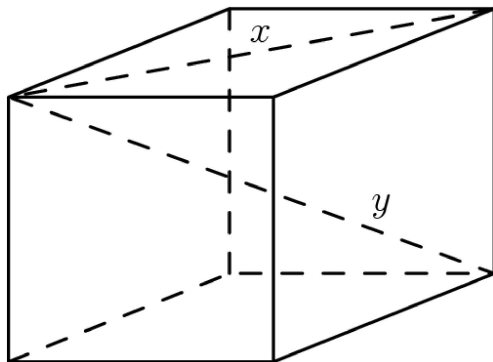
and CC was unchanged. For the second year, AA was down 20% from the previous year, BB was up 25% from the previous year, and CC was unchanged. If A, B, and C are the final values of the stock, then

- (A)  $A = B = C$     (B)  $A = B < C$     (C)  $C < B = A$   
 (D)  $A < B < C$     (E)  $B < A < C$

Solution

### Problem 17

A cube has eight vertices (corners) and twelve edges. A segment, such as  $x$ , which joins two vertices not joined by an edge is called a diagonal. Segment  $y$  is also a diagonal. How many diagonals does a cube have?



- (A) 6    (B) 8    (C) 12    (D) 14    (E) 16

Solution

### Problem 18

At the grocery store last week, small boxes of facial tissue were priced at 4 boxes for \$5. This week they are on sale at 5 boxes for \$4. The percent decrease in the price per box during the sale was closest to

- (A) 30%    (B) 35%    (C) 40%    (D) 45%    (E) 65%

Solution

### Problem 19

If the product  $\frac{3}{2} \cdot \frac{4}{3} \cdot \frac{5}{4} \cdot \frac{6}{5} \cdot \dots \cdot \frac{a}{b} = 9$ , what is the sum of  $a$  and  $b$ ?

- (A) 11    (B) 13    (C) 17    (D) 35    (E) 37

Solution

## Problem 20

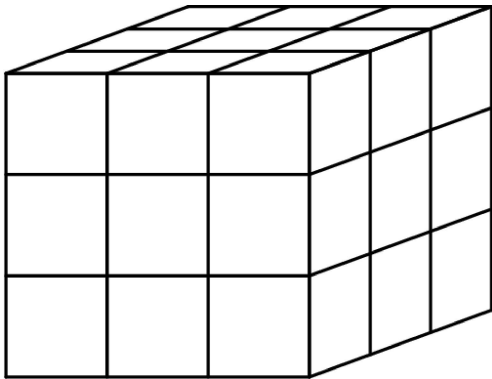
A pair of 8-sided dice have sides numbered 1 through 8. Each side has the same probability (chance) of landing face up. The probability that the product of the two numbers that land face-up exceeds 36 is

- (A)  $\frac{5}{32}$     (B)  $\frac{11}{64}$     (C)  $\frac{3}{16}$     (D)  $\frac{1}{4}$     (E)  $\frac{1}{2}$

Solution

## Problem 21

Each corner cube is removed from this  $3 \text{ cm} \times 3 \text{ cm} \times 3 \text{ cm}$  cube. The surface area of the remaining figure is



- (A) 19 sq.cm    (B) 24 sq.cm    (C) 30 sq.cm    (D) 54 sq.cm    (E) 72 sq.cm

Solution

## Problem 22

A two-inch cube ( $2 \times 2 \times 2$ ) of silver weighs 3 pounds and is worth \$200. How much is a three-inch cube of silver worth?

- (A) 300 dollars    (B) 375 dollars    (C) 450 dollars    (D) 560 dollars    (E) 675 dollars

Solution

## Problem 23

There are positive integers that have these properties:

- the sum of the squares of their digits is 50, and

- each digit is larger than the one to its left.

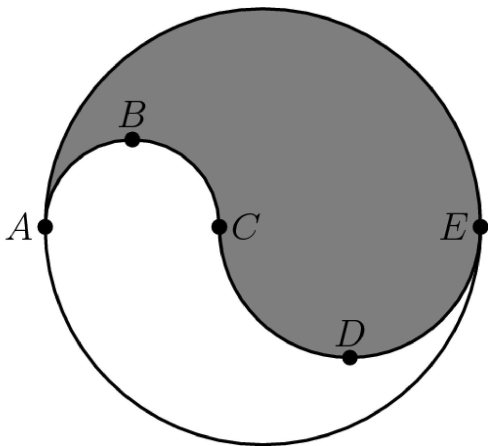
The product of the digits of the largest integer with both properties is

- (A) 7    (B) 25    (C) 36    (D) 48    (E) 60

Solution

### Problem 24

Diameter  $ACE$  is divided at  $C$  in the ratio  $2 : 3$ . The two semicircles,  $ABC$  and  $CDE$ , divide the circular region into an upper (shaded) region and a lower region. The ratio of the area of the upper region to that of the lower region is



- (A)  $2 : 3$     (B)  $1 : 1$     (C)  $3 : 2$     (D)  $9 : 4$     (E)  $5 : 2$

Solution

### Problem 25

All of the even numbers from 2 to 98 inclusive, excluding those ending in 0, are multiplied together. What is the rightmost digit (the units digit) of the product?

- (A) 0    (B) 2    (C) 4    (D) 6    (E) 8

Solution

# 1997 AJHSME Answer Key

1. C
2. D
3. B
4. E
5. A
6. C
7. D
8. B
9. C
10. C
11. A
12. D
13. A
14. D
15. B
16. E
17. E
18. B
19. D
20. A
21. D
22. E
23. C
24. C
25. D